

科目：控制系統 適用：電機所系統組

考生注意：

1. 依次序作答，只要標明題號，不必抄題。
2. 答案必須寫在答案卷上，否則不予計分。
3. 限用藍、黑色筆作答；試題須隨卷繳回。

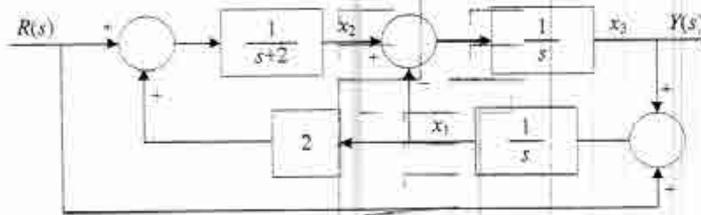
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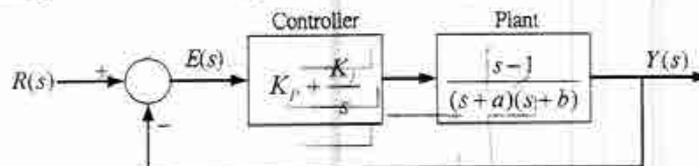
1. (30 pts.) Consider the dynamic system $\dot{x}(t) = Ax(t) + Bu(t)$ and $y(t) = Cx(t)$, where

$$A = \begin{bmatrix} -1 & 2 & 2 & -5 \\ 1 & 0 & -2 & 0 \\ 0 & 0 & -1 & 2 \\ 0 & 0 & -2 & -5 \end{bmatrix}, \quad B = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad \text{and} \quad C = [1 \quad 1 \quad 0 \quad 1].$$

- (a) (10 pts.) Is the system stable? Why?
 - (b) (10 pts.) Determine the transfer function from the input $u(t)$ to the output $y(t)$.
 - (c) (10 pts.) Determine the zero-state response of the system with unit step input.
2. (25 pts.) The block diagram of a system is shown in the following figure with the input $R(s)$, the output $Y(s)$ and the three state variables x_1 , x_2 and x_3 .



- (a) (10 pts.) Determine the transfer function of the system.
 - (b) (15 pts.) Is this system with the given state variables controllable or observable? Why?
3. (25 pts.) A unity feedback control system with a PI compensator is shown as follows:



- (a) (10 pts.) If $a = -b$ and $K_i = 0$, find the proportional gain K_p to stabilize the system.
 - (b) (15 pts.) If $a = b > 0$ and $K_p = K_i$, determine the value of K_p so that the steady-state error $\lim_{t \rightarrow \infty} e(t)$ for a unit step input is equal to zero.
4. (20 pts.) True or false? Justify your answers. (Give a brief proof or explanation if it is true. Otherwise, give a right correction or counter example if it is false).
- (a) (5 pts.) For a prototype 2^{nd} -order system, the maximum overshoot of its unit-step response and the resonant peak of the magnitude of its frequency response depend on both damping ratio and natural frequency.
 - (b) (5 pts.) A phase-lag compensator can provide a phase-lag angle and a significant attenuation over the frequency range of interest because it has a frequency response like an integrator over a finite range of frequencies.
 - (c) (5 pts.) If the characteristic equation of a closed-loop system is $(s+3)(s^2+9) = 0$, then the system is said to be marginally stable. That is to say, the system output will be sustained bounded oscillations for any bounded input.
 - (d) (5 pts.) The transfer function representation of a linear time-invariant system for input-output relationship is unique, so is the state-space representation.