

科目：結構學 適用：土木所耐震

考生注意：

1. 依次序作答，只要標明題號，不必抄題。
2. 答案必須寫在答案卷上，否則不予計分。
3. 限用藍、黑色筆作答；試題須隨卷繳回。

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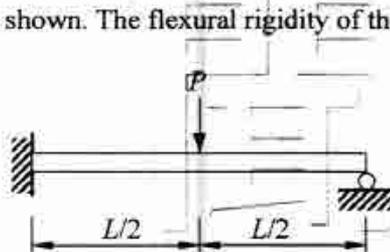
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1. The three equations of static equilibrium for an arbitrary planar structure are as follows

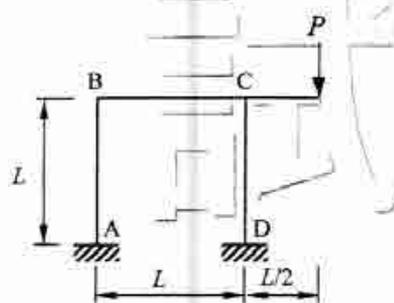
$$\sum P_y = 0; \quad \sum M_A = 0 \quad ; \quad \sum M_B = 0,$$

where the subscript  $y$  represents the  $y$  axis of a planar Cartesian  $x$ - $y$  coordinate system, and the subscript  $A$  and  $B$  represent two points on the  $xy$  plane. Please prove that, for the three equilibrium equations to be valid, the line connecting points  $A$  and  $B$  must not be perpendicular to the  $y$  axis (or, equivalently, must not be parallel to the  $x$  axis). (25%)

2. Please compute all the support reactions, the mid-span member forces and the mid-span deflection of the beam as shown. The flexural rigidity of the beam is  $EI$ . (25%)



3. Please compute and plot the bending moment diagram of the frame structure as shown. The flexural rigidity of all the structural members is  $EI$ . (25%)



4. Please derive the stiffness matrix for a planar beam element. The beam element should have 6 degrees of freedom. (25%)