

科目：控制系統 適用：電機所系統組

考生注意：

1. 依次序作答，只要標明題號，不必抄題。
2. 答案必須寫在答案卷上，否則不予計分。
3. 限用藍、黑色筆作答；試題須隨卷繳回。

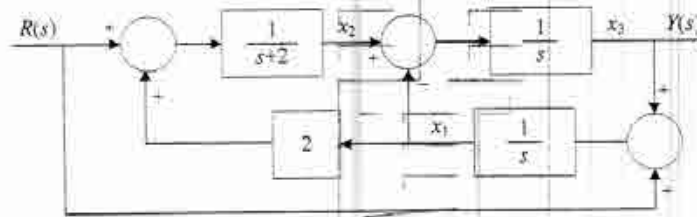
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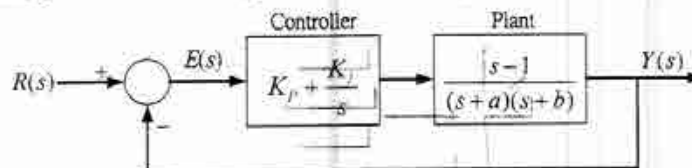
1. (30 pts.) Consider the dynamic system  $\dot{x}(t) = Ax(t) + Bu(t)$  and  $y(t) = Cx(t)$ , where

$$A = \begin{bmatrix} -1 & 2 & 2 & -5 \\ 1 & 0 & -2 & 0 \\ 0 & 0 & -1 & 2 \\ 0 & 0 & -2 & -5 \end{bmatrix}, \quad B = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad \text{and} \quad C = [1 \quad 1 \quad 0 \quad 1].$$

- (10 pts.) Is the system stable? Why?
  - (10 pts.) Determine the transfer function from the input  $u(t)$  to the output  $y(t)$ .
  - (10 pts.) Determine the zero-state response of the system with unit step input.
2. (25 pts.) The block diagram of a system is shown in the following figure with the input  $R(s)$ , the output  $Y(s)$  and the three state variables  $x_1$ ,  $x_2$  and  $x_3$ .



- (10 pts.) Determine the transfer function of the system.
  - (15 pts.) Is this system with the given state variables controllable or observable? Why?
3. (25 pts.) A unity feedback control system with a PI compensator is shown as follows:



- (10 pts.) If  $a = -b$  and  $K_i = 0$ , find the proportional gain  $K_p$  to stabilize the system.
  - (15 pts.) If  $a = b > 0$  and  $K_p = K_i$ , determine the value of  $K_p$  so that the steady-state error  $\lim_{t \rightarrow \infty} e(t)$  for a unit step input is equal to zero.
4. (20 pts.) True or false? Justify your answers. (Give a brief proof or explanation if it is true. Otherwise, give a right correction or counter example if it is false).
- (5 pts.) For a prototype 2<sup>nd</sup>-order system, the maximum overshoot of its unit-step response and the resonant peak of the magnitude of its frequency response depend on both damping ratio and natural frequency.
  - (5 pts.) A phase-lag compensator can provide a phase-lag angle and a significant attenuation over the frequency range of interest because it has a frequency response like an integrator over a finite range of frequencies.
  - (5 pts.) If the characteristic equation of a closed-loop system is  $(s+3)(s^2+9) = 0$ , then the system is said to be marginally stable. That is to say, the system output will be sustained bounded oscillations for any bounded input.
  - (5 pts.) The transfer function representation of a linear time-invariant system for input-output relationship is unique, so is the state-space representation.